Implications of the inter-period correlation of simulated ground motions on structural risk

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Outline

1. Introduction
2. Evaluation of Existing Ground Motion Simulation Methods
3. Correlation of $\epsilon$: Incorporation into SMSIM
4. Structural Fragility Example
5. Conclusions

What is the status of the simulations?
A partial fix!
Why does this matter?
1) Introduction

Definition:

Epsilon (\(\epsilon\)) is the number of standard deviations difference between the observed/simulated IM (i.e. Sa or FAS, in ln units) and the median model prediction (ln units); a normalized residual.

Question:

Why does the inter-period correlation of \(\epsilon\) (\(\rho_\epsilon\)) matter?

Answer:

\(\epsilon\) is an indicator of the peaks and troughs at a given frequency in a spectrum. 
\(\rho_\epsilon\) characterizes the relative width of these extrema.

We show that \(\rho_\epsilon\) is an essential component of simulated ground motions for capturing the variability of structural response that is needed in seismic fragility and seismic risk studies.
1) Introduction

**Example spectrum with high $\rho_\epsilon$**
(smoothed FAS)

**Example spectrum with low $\rho_\epsilon$**
(smoothed FAS)
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Others (Burks and Baker, 2014; Tothong and Cornell, 2006) have studied the inter-period correlation of response spectra from simulated ground motions – mixed results.

We focus in the Fourier Amplitude Spectra (FAS) domain to analyze the simulations and compare with the correlations in the data.

FAS provides the simulation developers better feedback to modify their methods that is not clear when using PSA.

Methods analyzed:

GP (Graves and Pitarka, 2015)
SDSU (Olsen and Takedatsu, 2015)
EXSIM (Atkinson and Assatourians, 2015)
UCSB (Crempien and Archuleta, 2015)
SONG (Song, 2016)
LLNL (Rodgers et al., 2018)
Pitarka (Pitarka et al., 2017)

SCEC BBP (1d)
3d finite difference
GP wave propagation (1d)
2) Evaluation of Existing Ground Motion Simulation Methods

Dashed: empirical FAS correlation model

Dashed: empirical PSA correlation model
2) Evaluation of Existing Ground Motion Simulation Methods

Dashed: empirical FAS correlation model

Dashed: empirical PSA correlation model
2) Evaluation of Existing Ground Motion Simulation Methods

Conclusions regarding correlation in simulations:

- None of the finite-fault simulation methods tested capture the total inter-period correlations over the entire frequency range evaluated, although several of the methods show promise at low frequencies.
  - By using a 1d velocity model, the BBP correlations are unable to capture the between-site component, which strongly contributes to the total correlation.

Implementation:

- Stochastic part: should be straight-forward (shown next)
- Deterministic part: more difficult – likely requires modifying the rupture generator or the wave propagation
  - changes to the rupture generator may be the most promising approach to modifying the long period inter-period correlations.
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3) Correlation of $\epsilon$: Incorporation into SMSIM

SMSIM (Boore, 2003)
3) Correlation of $\epsilon$: Incorporation into SMSIM

Steps to incorporate correlated $\epsilon$ into SMSIM:

- Generate zero-mean correlated random variables using a total correlation model for FAS (e.g. Bayless and Abrahamson, 2018 in prep)

- Scale the $\epsilon$ by the desired standard deviation

- Insert the correlated $\epsilon$ into step d of the SMSIM procedure and proceed as usual (shape to spectrum then inverse transform)
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4) Structural Fragility Example

We develop example structural fragilities using an IDA with two sets of ground motions created using the correlated and uncorrelated versions of SMSIM

Procedure:

1. Suites of 500 uncorrelated and correlated ground motions with the same median spectra

2. Perform incremental dynamic analysis (IDA) to get structural fragility functions: the probability of a structural consequence (EDP) as a function of the ground motion intensity
   - Structural models and dynamic nonlinear structural analyses using OpenSees (McKenna et al., 2010)

3. Combine structural fragilities with seismic hazard to calculate the EDP hazard

4. Compare results between suites of ground motions
4) Structural Fragility Example

Uncorrelated
(standard SMSIM)

SMSIM with correlation
4) Structural Fragility Example

Structural analysis results for both sets

MIDR>4% probabilities (symbols)
CDF fragility functions (lines)
4) Structural Fragility Example

In this example, a 43% increase in structural risk using the correlated version of SMSIM.
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5) Conclusions

- Without the adequate inter-period correlation in simulated ground motions, variability in the structural response may be under-estimated.

- This leads to structural fragilities which are too steep (under-estimated dispersion parameter $\beta$) and propagates through to non-conservative estimates of seismic risk.

Simulations:

- Using the correlation of the FAS provides the developers of the simulation methods better feedback in terms of how they can modify their methods that is not clear when using PSA comparisons.

- None of the six finite-fault simulation methods tested adequately capture the inter-period correlations over the entire frequency range evaluated, although several of the methods show promise at low frequencies.

- Changes to the rupture generator may be the most promising approach to modifying the long period inter-period correlations, if needed.
Thank you!

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